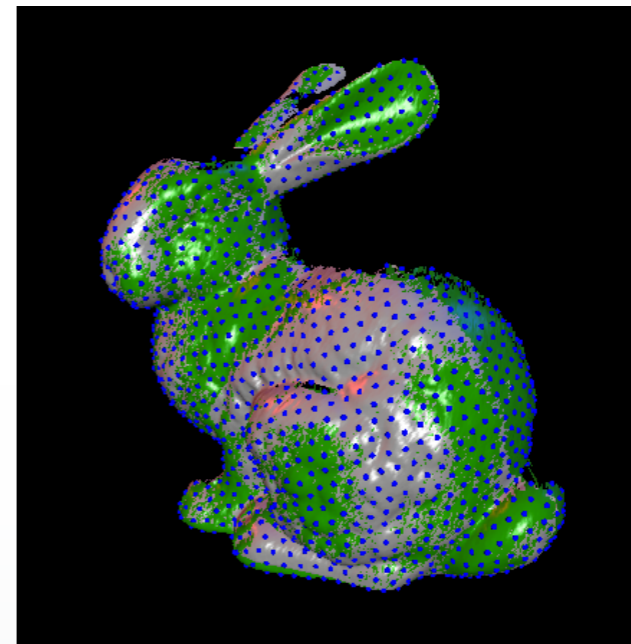


Exercise 2. Registration



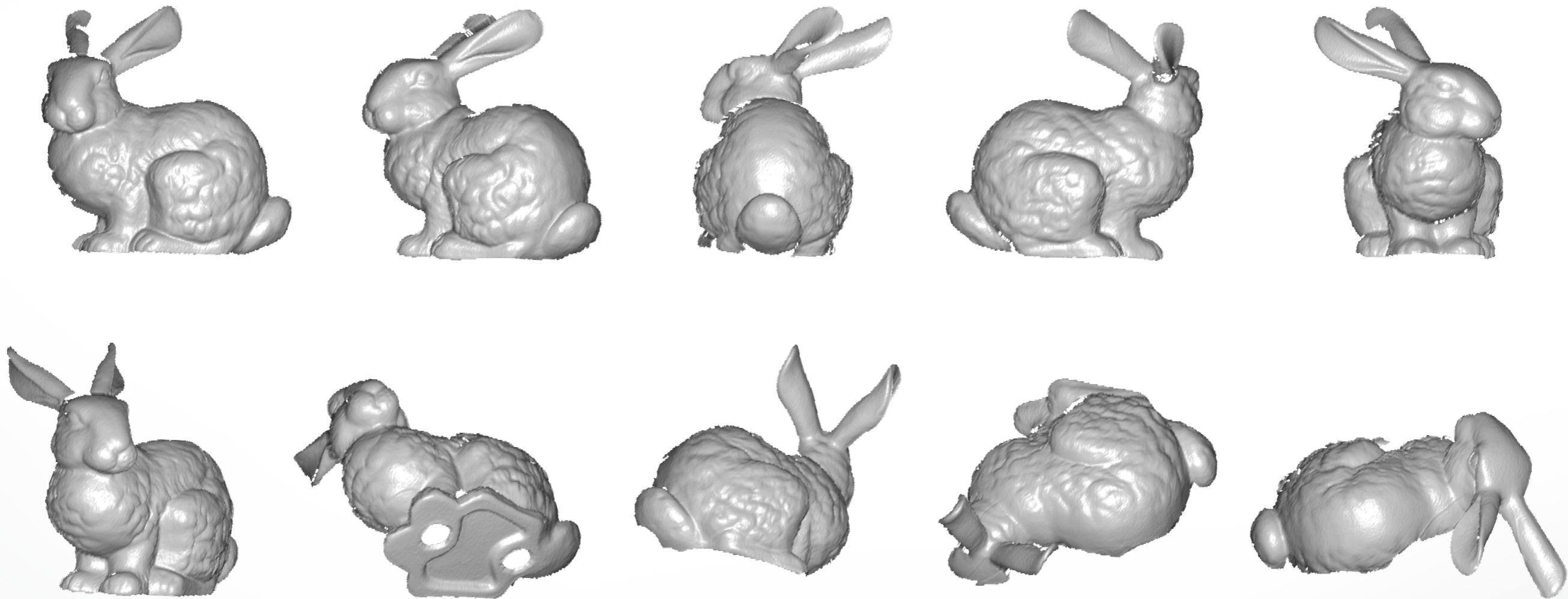
Tianye Li

Rigid Registration

- **Selecting** source points
- **Matching** points to the target mesh
- **Weighting** the correspondences
- **Rejecting** bad pairs
- Compute **error metric**
- **Minimize** error metric

Exercise 2

- Perform rigid registration between 10 scans of the Stanford bunny



Exercise 2

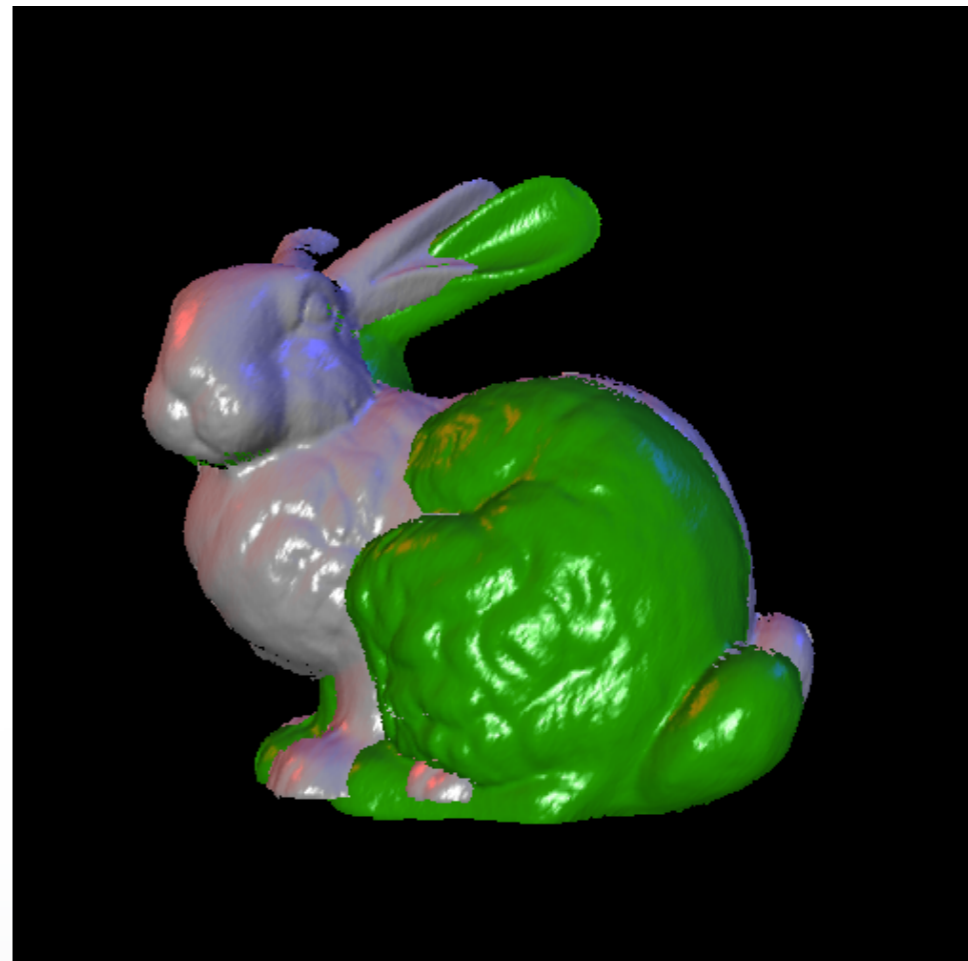
- Demo
 - `'SHIFT'` + mouse controls: manual alignment for an initial transformation
 - `'r'`: perform single registration step with point to point distance minimization
 - `'SPACE'`: perform single registration step with point to plane distance minimization
 - `'n'`: load next scan

Exercise 2

- Getting it compiled
- Subsampling
- Bad pairs rejection
- Point to point optimization
- Point to plane optimization

Getting It Compiled

- CMake, OpenGL, OpenMesh
- ANN (Approximate Nearest Neighbor)
 - efficient closest point lookup using kd-tree



Subsampling

- Uniform subsampling within a given radius
`subsampleRadius`
- `RegistrationViewer::subsample()` in
`RegistrationViewer.cc`



Bad Pairs Rejection

- Closest points are computed using ANN
- Prune correspondences based on
 - distance threshold
 - normal compatibility
- `RegistrationViewer::calculate_correspondences ()` in `RegistrationViewer.cc`

Point to Point Optimization

- Minimize $E = \sum_{i=1}^N \|\mathbf{R}\mathbf{p}_i + \mathbf{t} - \mathbf{q}_i\|_2^2$

by solving a linear system $\mathbf{Ax} = \mathbf{b}$

- `Registration::register_point2point()` in `Registration.cc`

Euler Angles

- Three elemental rotations:

$$\mathbf{R}_x(\alpha) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha \\ 0 & \sin \alpha & \cos \alpha \end{bmatrix} \quad \mathbf{R}_y(\beta) = \begin{bmatrix} \cos \beta & 0 & \sin \beta \\ 0 & 1 & 0 \\ -\sin \beta & 0 & \cos \beta \end{bmatrix} \quad \mathbf{R}_z(\gamma) = \begin{bmatrix} \cos \gamma & -\sin \gamma & 0 \\ \sin \gamma & \cos \gamma & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

- Any rotation matrix can be decomposed as a product of elemental three rotation matrix

$$\mathbf{R} = \mathbf{R}_z(\gamma)\mathbf{R}_y(\beta)\mathbf{R}_x(\alpha) = \begin{bmatrix} c_\gamma c_\beta & -c_\alpha s_\gamma + c_\gamma s_\beta s_\alpha & s_\gamma s_\alpha + c_\gamma c_\alpha s_\beta \\ c_\beta s_\gamma & c_\gamma c_\alpha + s_\gamma s_\beta s_\alpha & c_\alpha s_\gamma s_\beta - c_\gamma s_\alpha \\ -s_\beta & c_\beta s_\alpha & c_\beta c_\alpha \end{bmatrix}$$

$$c_\alpha = \cos \alpha \quad s_\alpha = \sin \alpha$$

Linearized Transformation

- Linearized Euler angle

(assuming small rotation: $\cos \alpha = 1$ $\sin \alpha = \alpha$)

$$\mathbf{R} = \begin{bmatrix} c_\gamma c_\beta & -c_\alpha s_\gamma + c_\gamma s_\beta s_\alpha & s_\gamma s_\alpha + c_\gamma c_\alpha s_\beta \\ c_\beta s_\gamma & c_\gamma c_\alpha + s_\gamma s_\beta s_\alpha & c_\alpha s_\gamma s_\beta - c_\gamma s_\alpha \\ -s_\beta & c_\beta s_\alpha & c_\beta c_\alpha \end{bmatrix} = \begin{bmatrix} 1 & -\gamma & \beta \\ \gamma & 1 & -\alpha \\ -\beta & \alpha & 1 \end{bmatrix}$$

- Linearized transformation

$$\mathbf{x} = [\alpha \quad \beta \quad \gamma \quad \mathbf{t}_x \quad \mathbf{t}_y \quad \mathbf{t}_z]^\top$$

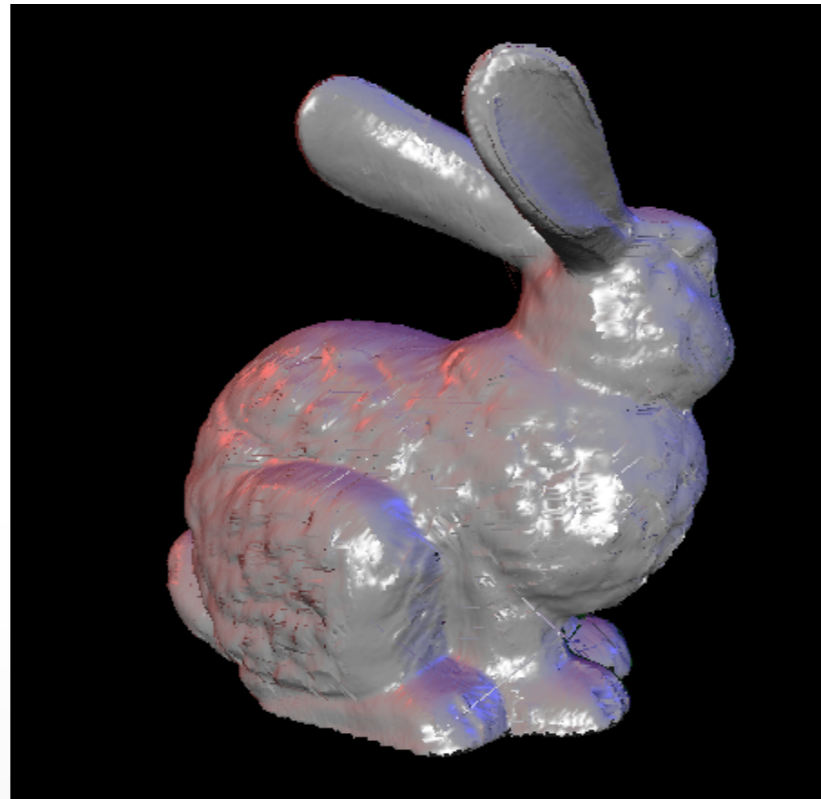
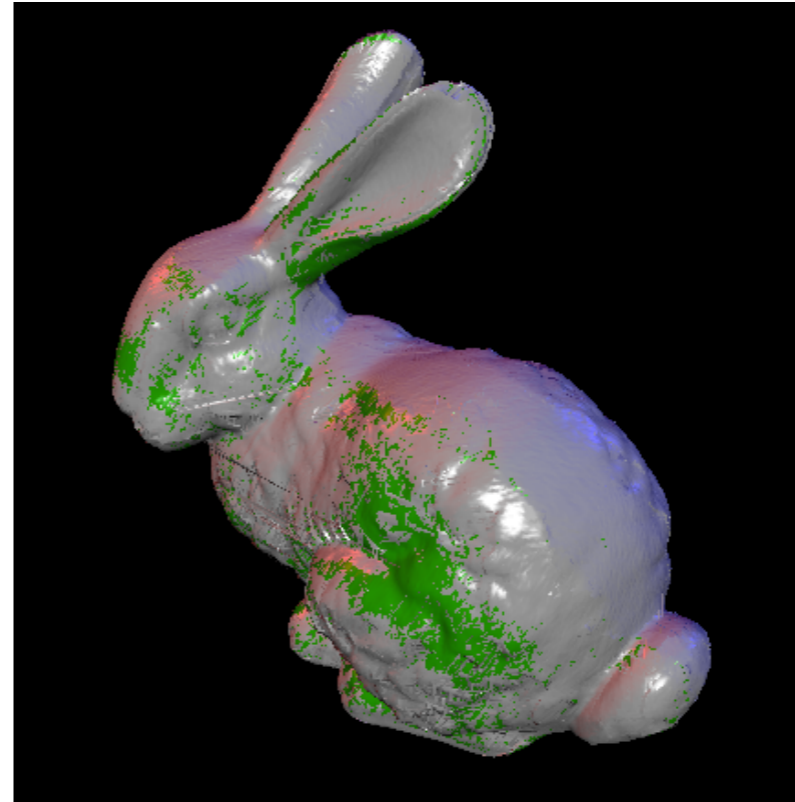
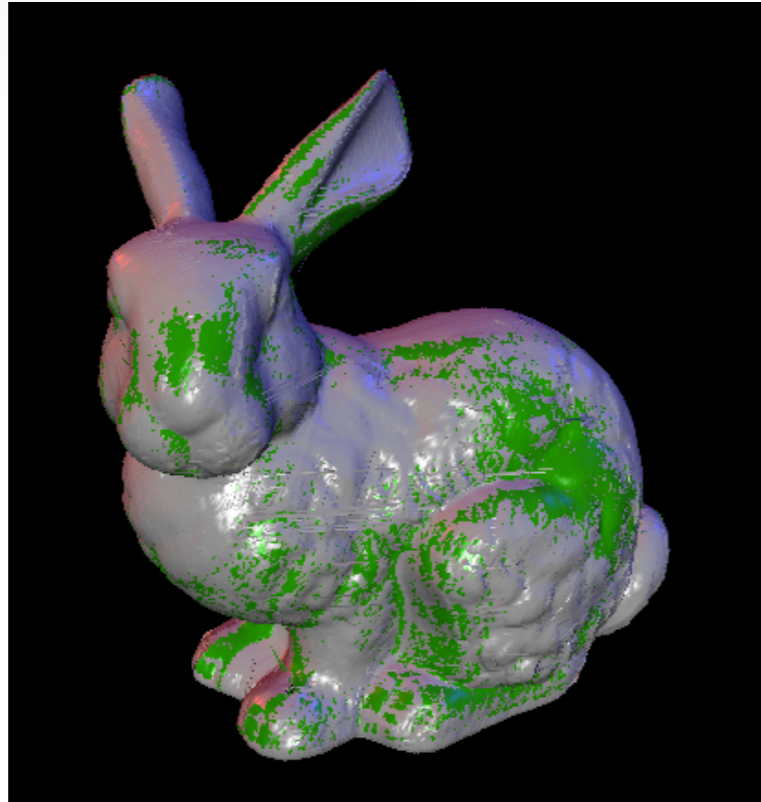
Point to Plane Optimization

- Minimize $E = \sum_{i=1}^N \|\mathbf{n}_i^\top (\mathbf{R}\mathbf{p}_i + \mathbf{t} - \mathbf{q}_i)\|_2^2$

by solving a linear system $\mathbf{Ax} = \mathbf{b}$

- `Registration::register_point2surface()` in `Registration.cc`

Results



Submission

- Deadline: **Feb 20, 2018 12:00pm (noon)**
- Upload a .zip compressed file named “Exercise2-YourName.zip” to
 - Blackboard
- Include a “read.txt” file describing how you solve each exercise and the encountered problems

Contact

- Office Hours: Monday 15:00 - 16:00 PHE 108
- email: tianyeli@usc.edu

Thanks!

