#### Fall 2018 CSCI 420 Computer Graphics

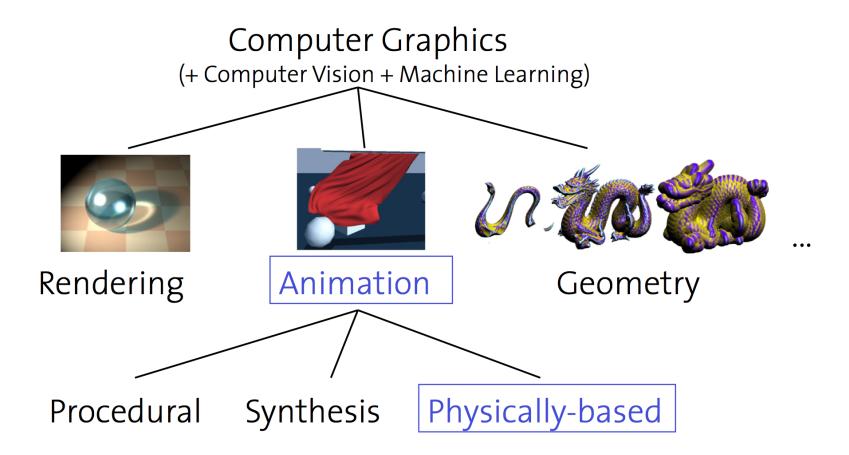
# 13.1 Physically Based Simulation I





http://cs420.hao-li.com

# **Visual Computing**



# Animation

- Animation from *anima* (lat.)
  = soul, spirit, breath of life
- Bring images to life!
- Examples
  - Character animation (humans, animals)



- Secondary motion (hair, cloth)
- Physical world (rigid bodies, water, fire)

# **Animation Techniques**

- For character animation
  - Keyframing
  - Motion capturing / motion synthesis
- For secondary motion, physical effects
  - Procedural
  - Simulation (physically based animation)

# **Physics in Computer Graphics**

#### • Very common

- Computer Animation, Modeling (computational mechanics)
- Rendering (computational optics)





# **Physics in Computer Animation**

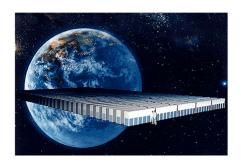
- Fluids
- Smoke
- Deformable strands (rods)
- Cloth
- Solid 3D deformable objects .... and many more!





# **Physical Simulation**

- Equations known for a long time
  - Motion (Newton, 1660)
  - Elasticity (Hooke, 1670)
  - Fluids (Navier, Stokes, 1822)
- Simulation made possible by computers
  - 1938: Zuse 1, 0.2 flops,
  - 2008: Roadrunner, 122k cores, 1026 teraflops



$$d/dt(m\mathbf{v}) = \mathbf{f}$$

 $\sigma = E\epsilon$ 

$$\rho\left(\frac{\partial \mathbf{v}}{\partial t} + \mathbf{v} \cdot \nabla \mathbf{v}\right) = -k\nabla \rho + \rho \mathbf{g} + \mu \nabla^2 \mathbf{v}$$

# **Scientific Goals and Challenges**

- Goal of scientific computations
  - Reproduction of physical phenomena
  - Substitute for real experiments
- Goal of physically-based animation
  - Imitation of physical phenomena
  - Visually plausible behavior
  - As much realism as possible within performance and stability constraints

→Different goals require different methods/ representations...

# **Offline Physics**

- Special effects (film, commercials)
- Large models: millions of particles / tetrahedra / triangles
- Use computationally expensive rendering (global illumination)
- Impressive results
- Many seconds of computation time per frame

# **Real-time Physics**

- Interactive systems: computer games virtual medicine (surgical simulation)
- Must be fast (30 fps, preferably 60 fps for games) Only a small fraction of CPU time devoted to physics!
- Has to be stable, regardless of user input

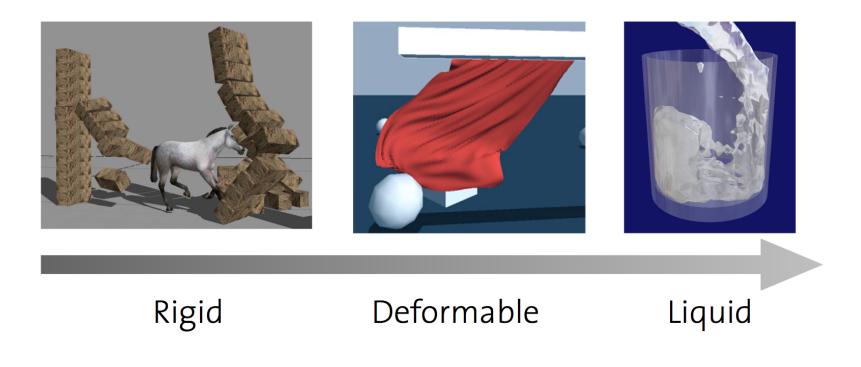


Flight/car Simulators





### Examples



### Fluids



Enright, Marschner, Fedkiw, SIGGRAPH 2002

### **Fluids and Rigid Bodies**



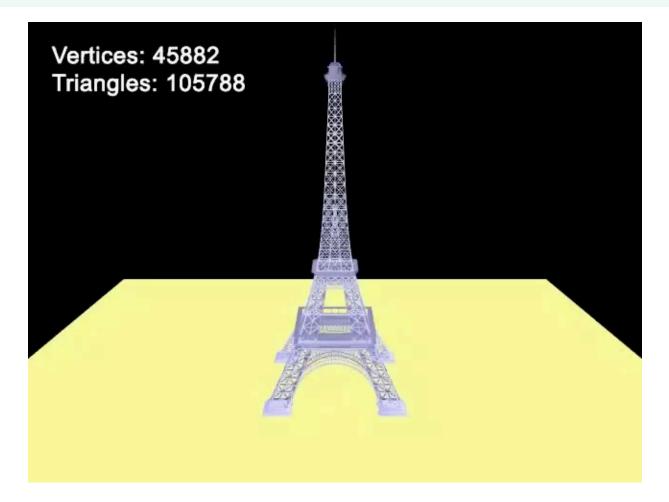
#### Fluids with Deformable Solid Coupling

[Robinson-Mosher, Shinar, Gretarsson, Su, Fedkiw, SIGGRAPH 2008]

#### Two-way Coupling of Fluids to Rigid and Deformable Solids and Shells

Avi Robinson-Mosher Tamar Shinar Jon Gretarsson Jonathan Su Ronald Fedkiw

### **Deformations**

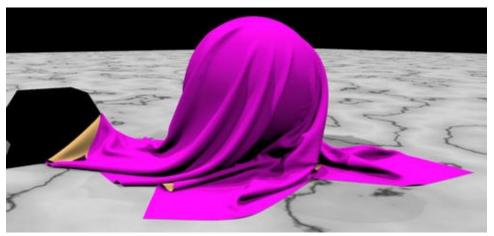


[Barbic and James, SIGGRAPH 2005]

# Cloth

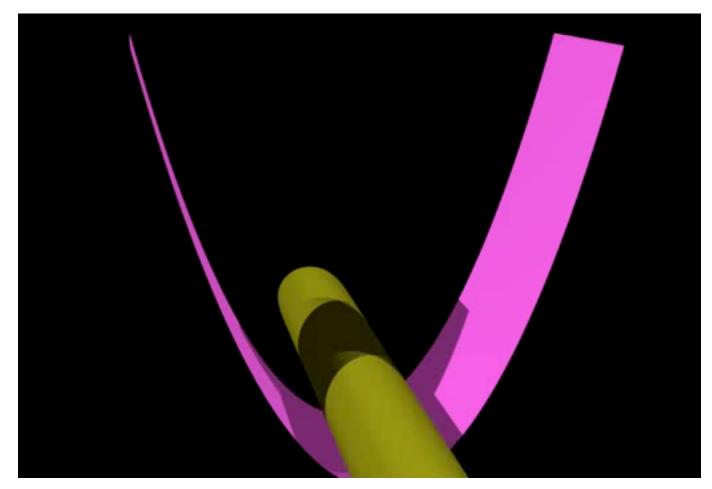


#### Source: ACM SIGGRAPH



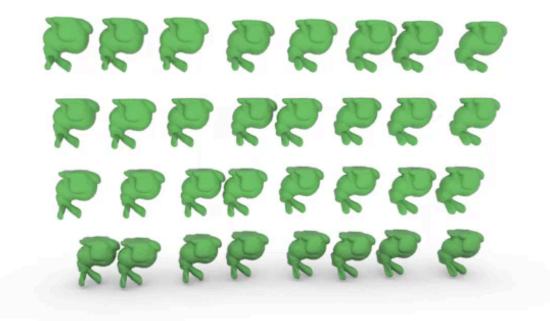


# Cloth (Robustness)



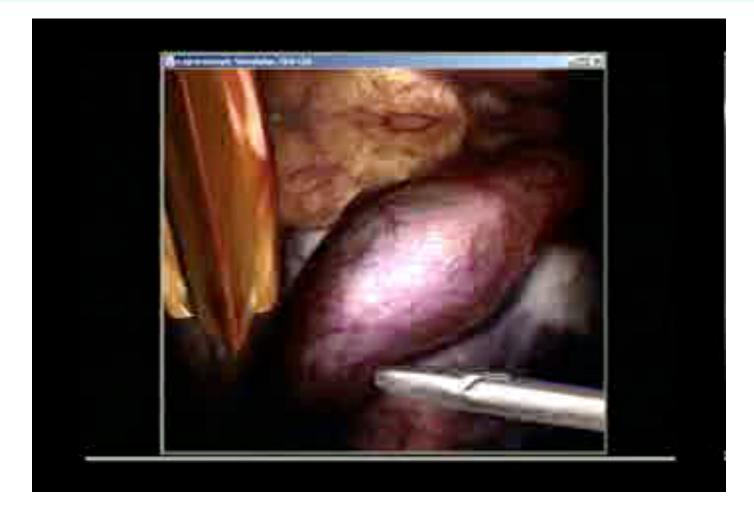
[Bridson, Fedkiw, Anderson, ACM SIGGRAPH 2002

## Multibody Dynamics + Self-collision Detection



[Barbic and James, SIGGRAPH 2010]

## **Surgical Simulation**



[James and Pai, SIGGRAPH 2002]

# **Multibody Dynamics**

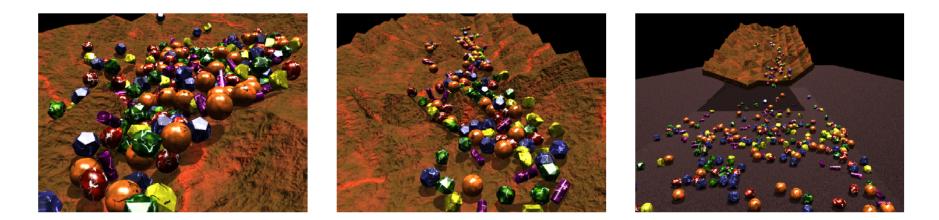


Figure 1: Avalanche: 300 rocks tumble down a mountainside.

### **Physics in Games**

Real-Time Deformation and Fracture in a Game Environment

> Eric Parker Pixelux Entertainment

> > James O'Brien U.C. Berkeley

Video Edited by Sebastian Burke

From the proceedings of SCA 2009, New Orleans

[Parker and James, Symposium on Computer Animation 2009]

# **Sound Simulation (Acoustics)**



[James, Barbic, Pai, SIGGRAPH 2006]

# Techniques

- Particle systems
  - Fire, smoke, water ...
- Mass-spring systems
  - Deformable objects, cloth ...
- Rigid body simulation
  - Cars, airplanes, furniture ...
- Grid based methods
  - Water, smoke, airflow ...
- Finite Elements
  - Accurate deformable objects ...

### **Particle System**





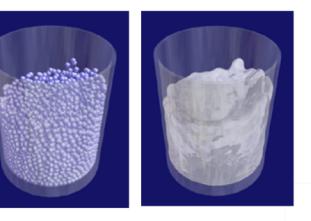


Snow, dust, sand



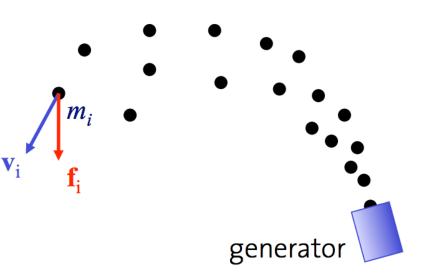
Smoke

Water



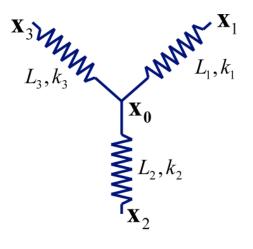
# **Particle System**

- Collection of many small simple particles
- Particle motion influenced by forces
- Generated by emitters
- Deleted when lifetime reached or out of scene



# **Mass-Spring Systems**

- Particle system + springs
- Special interaction force
- Issues:
  - Where to put springs
  - Choice of stiffnesses
  - Collision detection
  - Collision response
  - Stability (time step or stiffness too high)



# **Applications**

#### Facial animation







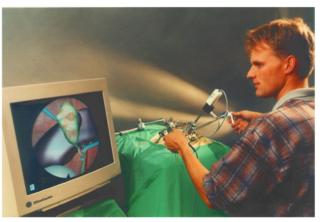
#### Thalmann

#### Cloth simulation



Strasser

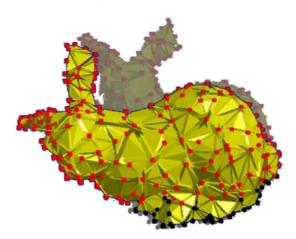
#### Surgery simulation



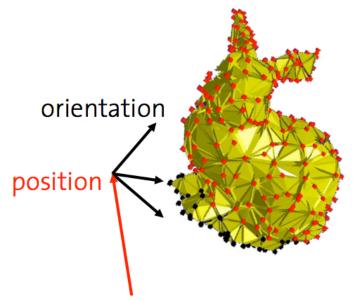
Kuehnapfel

# **Rigid Body Simulation**

- Deformable objects have many degrees of freedom
- Each vertex is simulated separately



- A rigid body only has 6 degrees of freedom
- Faster simulation possible



# Challenges

- Collision detection
- Collision response for complex configurations
- Constraints (joints)



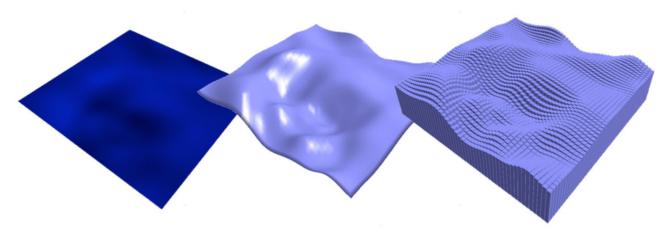


# **Applications**

- Robotic simulations
- 3D computer games



#### **Grid-Based Methods**



- Basic idea:
  - Solve partial differential equation on (regular) grid
  - Replace differentials by finite differences

# **Example: Fluid Surface**

- Water surface defined as height *u(x,y,t)* at location *x,y* at time *t*
- Dynamics given by 2D wave eqn:

$$\frac{\partial^2}{\partial t^2}u = c^2\left(\frac{\partial^2}{\partial x^2}u + \frac{\partial^2}{\partial y^2}u\right)$$

• Discretization:

$$v^{t+1}[i,j] = v^t[i,j] + \Delta t \, c^2 \, \frac{u^t[i+1,j] + u^t[i-1,j] + u^t[i,j+1] + u^t[i,j-1] - 4u^t[i,j]}{h^2}$$

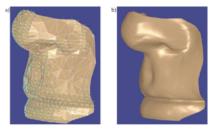
u(x,y,t)

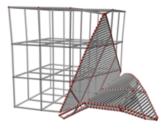
(x, v)

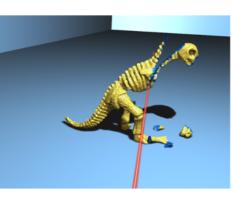
 $u^{t+1}[i, j] = u^{t}[i, j] + \Delta t v^{t+1}[i, j]$ 

# **FEM Simulation**

- Discretize equations from continuum mechanics
- Solve (more) accurately
- Independent of tesselation
- Volumetric meshes

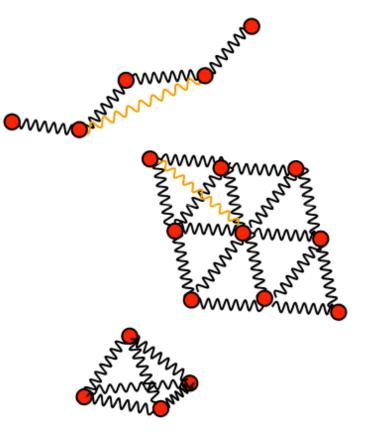






#### **Case Study: Mass-spring Systems**

- Mass particles connected by elastic springs
- One dimensional: rope, chain
- Two dimensional: cloth, shells
- Three dimensional: soft bodies



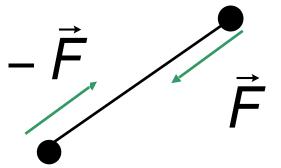
Source: Matthias Mueller, SIGGRAPH

## **Newton's Laws**

• Newton's 2nd law:

 $\vec{F} = m\vec{a}$ 

- Gives acceleration, given the force and mass
- Newton's 3rd law: If object A exerts a force F on object B, then object B is at the same time exerting force -F on A

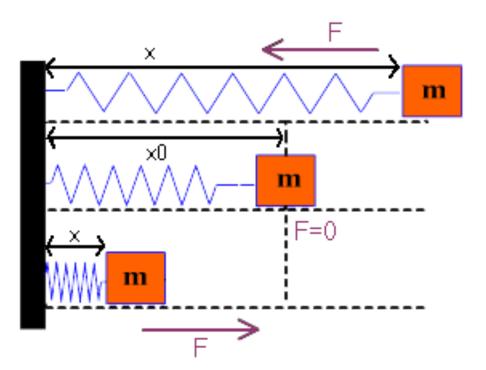


# Single spring

• Obeys the *Hook's law*:

 $\mathsf{F} = \mathsf{k} (\mathsf{x} - \mathsf{x}_0)$ 

- $x_0 = rest length$
- k = spring elasticity (*stiffness*)
- For x<x<sub>0</sub>, spring wants to extend
- For x>x<sub>0</sub>, spring wants to contract



## Hook's law in 3D

- Assume A and B two mass points connected with a spring.
- Let L be the vector pointing from B to A
- Let R be the spring rest length
- Then, the elastic force exerted on A is:

$$\vec{F} = -k_{Hook}(|\vec{L}| - R)\frac{\vec{L}}{|\vec{L}|}$$

# Damping

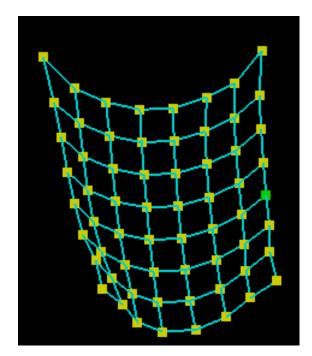
- Springs are not completely elastic
- They absorb some of the energy and tend to decrease the velocity of the mass points attached to them
- Damping force depends on the velocity:

$$\vec{F} = -k_d \vec{V} \qquad \overbrace{\mathsf{rest length}}^{\mathsf{x}} \qquad \overbrace{\mathsf{F}_{\mathsf{Damping}}}^{\mathsf{x}} \qquad \overbrace{\mathsf{F}_{\mathsf{D}}} \qquad \overbrace{\mathsf{F}_{\mathsf{D}}}^{\mathsf{x}} \qquad \overbrace{\mathsf{F}_{\mathsf{D}}} \qquad \overbrace{\mathsf{D}} \qquad \overbrace{\mathsf{F}_{\mathsf{D}}} \qquad \overbrace{\mathsf{D}} \ \overbrace{\mathsf{D}} \ \overbrace{\mathsf{D}} \ \scriptsize{\mathsf{D}}} \qquad \overbrace{\mathsf{D}} \ \overbrace{\mathsf{D}} \ \scriptsize{\mathsf{D}} \ \scriptsize{\mathsf{D}} \ \scriptsize{\mathsf{D}} \ \scriptsize{\mathsf{D}} \ \scriptsize{\mathsf{D}}} \qquad \overbrace{\mathsf{D}} \ \scriptsize{\mathsf{D}} \ \scriptsize{\mathsf{D}}} \ \scriptsize$$

- k<sub>d</sub> = damping coefficient
- k<sub>d</sub> different than k<sub>Hook</sub> !!

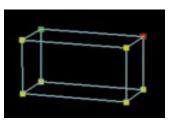
# A network of springs

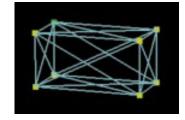
- Every mass point connected to some other points by springs
- Springs exert forces on mass points
  - Hook's force
  - Damping force
- Other forces
  - External force field
    - Gravity
    - Electrical or magnetic force field
  - Collision force



#### Network organization is critical

• For stability, must organize the network of springs in some clever way





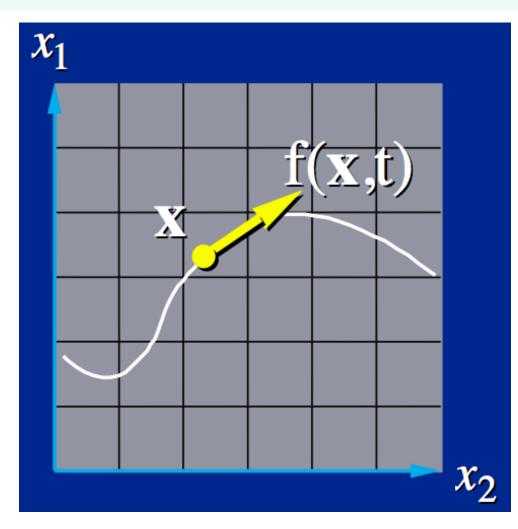


Basic network

Stable network

Network out of control

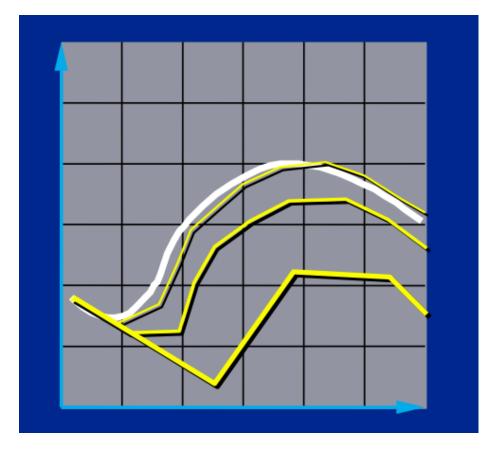
## **Time Integration**



Physics equation: x' = f(x,t)

x=x(t) is particle trajectory

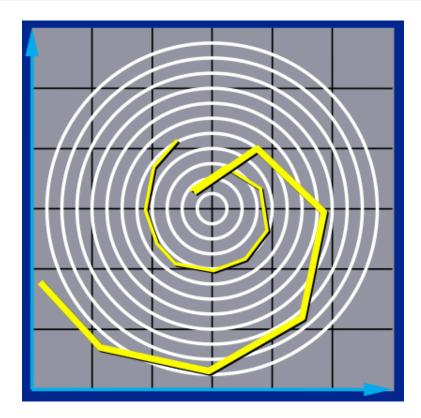
#### **Euler Integration**

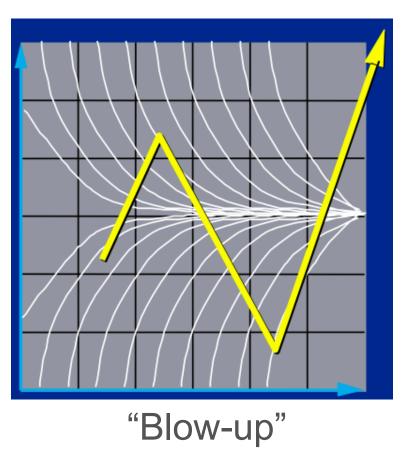


#### Simple, but inaccurate.

Unstable with large timesteps.

#### **Inaccuracies with explicit Euler**

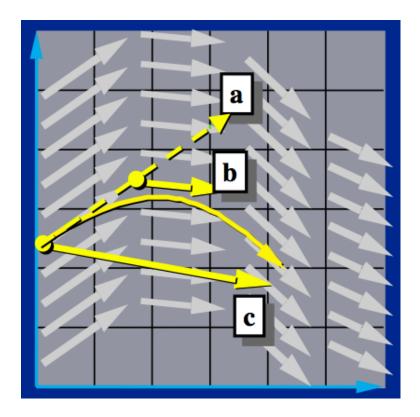




#### Gain energy

Source: Andy Witkin, SIGGRAPH

## **Midpoint Method**



Source: Andy Witkin, SIGGRAPH

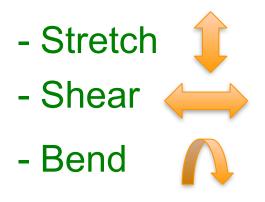
Improves stability

- 1. Compute Euler step  $\Delta x = \Delta t f(x, t)$
- 2. Evaluate f at the midpoint  $f_{mid} = f((x+\Delta x)/2, (t+\Delta t)/2)$
- 3. Take a step using the midpoint value  $x(t + \Delta t) = x(t) + \Delta t f_{mid}$

#### Many more methods

- Runge-Kutta (4th order and higher orders)
- Implicit methods
  - sometimes unconditionally stable
  - very popular (e.g., cloth simulations)
  - a lot of damping with large timesteps
- Symplectic methods
  - exactly preserve energy, angular momentum and/or other physical quantities
  - Symplectic Euler

#### **Cloth Simulation**

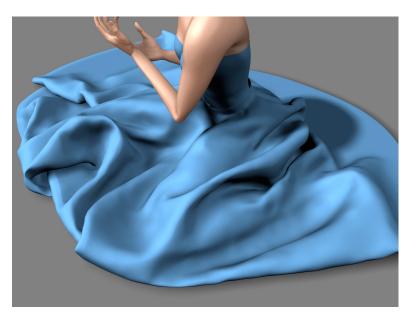




[Baraff and Witkin, SIGGRAPH 1998]

## Challenges

- Complex Formulas
- Large Matrices
- Stability
- Collapsing triangles
- Self-collision detection

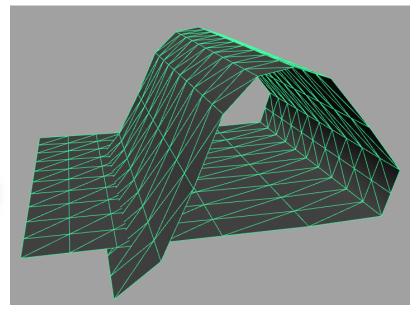


[Govindaraju et al. 2005]

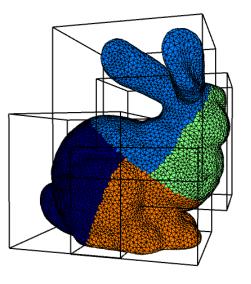
#### **Self-collisions: definition**

Deformable model is self-colliding iff

there exist non-neighboring intersecting triangles.

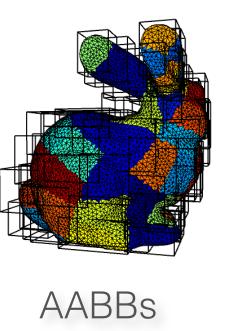


## **Bounding volume hierarchies**



AABBs

Level 1



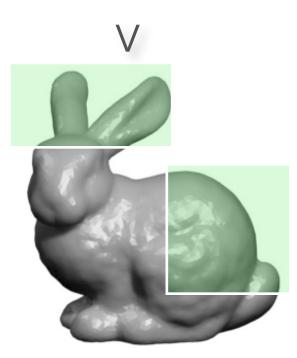
Level 3

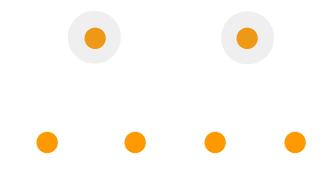
[Hubbard 1995] [Gottschalk et al. 1996] [van den Bergen 1997] [Bridson et al. 2002] [Teschner et al. 2002] [Govindaraju et al. 2005]

#### **Bounding volume hierarchy**



## **Bounding volume hierarchy**





#### **Real-time cloth simulation**



Source: Andy Pierce

52

Model	Triangles	FPS	% Forces + Stiffness Matrix	% Solver
Curtain	2400	25	67	33

http://cs420.hao-li.com

# Thanks!

